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On Terpolymerization Theory
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## LETTER TO THE EDITOR

## On Terpolymerization Theory

For systems of three monomers Ham (1) has proposed that the relation

$$
\begin{equation*}
P_{\mathrm{ab}} P_{\mathrm{bc}} P_{\mathrm{ca}}=P_{\mathrm{ac}} P_{\mathrm{cb}} P_{\mathrm{ba}} \tag{1}
\end{equation*}
$$

should hold but no theoretical proof was given. Here $P_{\mathrm{ab}}$ is the probability of monomer $\mathbf{B}$ adding to a chain ending in monomer A in the presence of monomers, $\mathrm{A}, \mathrm{B}$, and C , and so on.

In the present note we wish to derive Eq. (1) from the assumption that any special interactions between $A \cdot$ and $B$ and between $B$ and A (and so on) are symmetrical. From this assumption, we have

$$
\begin{align*}
& N_{\mathrm{ab}}=N_{\mathrm{ba}}  \tag{2}\\
& N_{\mathrm{bc}}=N_{\mathrm{cb}}  \tag{3}\\
& N_{\mathrm{ca}}=N_{\mathrm{ac}} \tag{4}
\end{align*}
$$

where $N_{\mathrm{ab}}$ and $N_{\mathrm{ba}}$ refer to the percentages of linkages of AB and BA in the copolymer, and so on.
The percentage of AB linkages in the copolymer is given by

$$
\begin{equation*}
N_{\mathrm{ab}}=a P_{\mathrm{ab}} \tag{5}
\end{equation*}
$$

Similarly,

$$
\begin{equation*}
N_{\mathrm{ba}}=b P_{\mathrm{ba}} \tag{6}
\end{equation*}
$$

where $a$ and $b$ refer to the molar percentages of monomer units in the copolymer. We have, therefore,

$$
\begin{equation*}
a P_{\mathrm{ab}}=b P_{\mathrm{ba}} \tag{7}
\end{equation*}
$$

Similarly, two other equations can be derived:

$$
\begin{gather*}
b P_{\mathrm{bc}}=c P_{\mathrm{cb}}  \tag{8}\\
c P_{\mathrm{ca}}=a P_{\mathrm{ac}}  \tag{9}\\
\quad 559
\end{gather*}
$$

Then the product of left sides of Eqs. (7) to (9) is

$$
\begin{equation*}
\left(a P_{\mathrm{ab}}\right)\left(b P_{\mathrm{bc}}\right)\left(c P_{\mathrm{ca}}\right) \tag{10}
\end{equation*}
$$

The product of right sides of Eqs. (7) to (9) is

$$
\begin{equation*}
\left(b P_{\mathrm{ba}}\right)\left(c P_{\mathrm{cb}}\right)\left(a P_{\mathrm{ac}}\right) \tag{11}
\end{equation*}
$$

As Eq. (10) is equivalent to Eq. (11), it can be shown that

$$
\begin{equation*}
\left(a P_{\mathrm{ab}}\right)\left(b P_{\mathrm{bc}}\right)\left(c P_{c a}\right)=\left(b P_{\mathrm{ba}}\right)\left(c P_{c b}\right)\left(a P_{\mathrm{ac}}\right) \tag{12}
\end{equation*}
$$

Dividing both sides by (abc) yields

$$
\begin{equation*}
P_{\mathrm{ab}} P_{\mathrm{bc}} P_{\mathrm{ca}}=P_{\mathrm{ac}} P_{\mathrm{cb}} P_{\mathrm{ba}} \tag{1}
\end{equation*}
$$

If steady-state concentrations of chain ends can be assumed for systems of three monomers, it can be proved that

$$
\begin{align*}
& N_{\mathrm{ab}}+N_{\mathrm{ac}}=N_{\mathrm{ba}}+N_{\mathrm{ca}}  \tag{13}\\
& N_{\mathrm{ba}}+N_{\mathrm{bc}}=N_{\mathrm{ab}}+N_{\mathrm{cb}} \tag{14}
\end{align*}
$$

If $N_{\mathrm{ab}}=N_{\mathrm{ba}}$, the following relations are shown, from Eqs. (13) and (14):

$$
\begin{align*}
& N_{\mathrm{bc}}=N_{\mathrm{cb}}  \tag{3}\\
& N_{\mathrm{ac}}=N_{\mathrm{ca}} \tag{4}
\end{align*}
$$

Therefore, Eq. (1) can be true only when $N_{\mathrm{ab}}=N_{\mathrm{ba}}$.

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1. G. E. Ham, J. Polymer Sci., A2, 2735 (1964).

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