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#### **On Terpolymerization Theory**

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J. MACROMOL. SCI. (CHEM.), A1(3), 559-560 (1967)

## LETTER TO THE EDITOR

## **On Terpolymerization Theory**

For systems of three monomers Ham (1) has proposed that the relation

$$P_{ab}P_{bc}P_{ca} = P_{ac}P_{cb}P_{ba} \tag{1}$$

should hold but no theoretical proof was given. Here  $P_{ab}$  is the probability of monomer B adding to a chain ending in monomer A in the presence of monomers, A, B, and C, and so on.

In the present note we wish to derive Eq. (1) from the assumption that any special interactions between A and B and between Band A (and so on) are symmetrical. From this assumption, we have

$$N_{\rm ab} = N_{\rm ba} \tag{2}$$

$$N_{\rm bc} = N_{\rm cb} \tag{3}$$

$$N_{\rm ca} = N_{\rm ac} \tag{4}$$

where  $N_{ab}$  and  $N_{ba}$  refer to the percentages of linkages of AB and BA in the copolymer, and so on.

The percentage of AB linkages in the copolymer is given by

$$N_{\rm ab} = aP_{\rm ab} \tag{5}$$

Similarly,

$$N_{\rm ba} = bP_{\rm ba} \tag{6}$$

where a and b refer to the molar percentages of monomer units in the copolymer. We have, therefore,

$$aP_{\rm ab} = bP_{\rm ba} \tag{7}$$

Similarly, two other equations can be derived:

$$bP_{\rm bc} = cP_{\rm cb} \tag{8}$$

$$cP_{ca} = aP_{ac} \tag{9}$$

Then the product of left sides of Eqs. (7) to (9) is

$$(aP_{ab})(bP_{bc})(cP_{ca})$$
 (10)

The product of right sides of Eqs. (7) to (9) is

$$(bP_{\rm ba})(cP_{\rm cb})(aP_{\rm ac}) \tag{11}$$

As Eq. (10) is equivalent to Eq. (11), it can be shown that

$$(aP_{ab})(bP_{bc})(cP_{ca}) = (bP_{ba})(cP_{cb})(aP_{ac})$$
(12)

Dividing both sides by (abc) yields

$$P_{ab}P_{bc}P_{ca} = P_{ac}P_{cb}P_{ba} \tag{1}$$

If steady-state concentrations of chain ends can be assumed for systems of three monomers, it can be proved that

$$N_{\rm ab} + N_{\rm ac} = N_{\rm ba} + N_{\rm ca} \tag{13}$$

$$N_{\rm ba} + N_{\rm bc} = N_{\rm ab} + N_{\rm cb} \tag{14}$$

If  $N_{ab} = N_{ba}$ , the following relations are shown, from Eqs. (13) and (14):

$$N_{\rm bc} = N_{\rm cb} \tag{3}$$

$$N_{\rm ac} = N_{\rm ca} \tag{4}$$

Therefore, Eq. (1) can be true only when  $N_{ab} = N_{ba}$ .

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